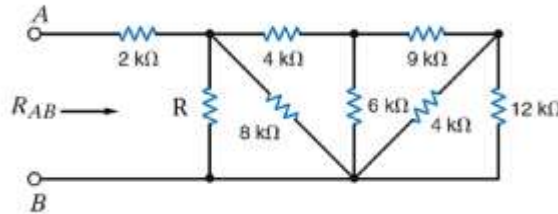


American University of Beirut
Department of Electrical and Computer Engineering
EECE 210 – Electric Circuits - Fall 2018
Quiz 1 Solutions

Problem 1 (4 pts)

If $R = 8 \text{ k}\Omega$, find the equivalent resistance, R_{AB} .



$$R_{AB} = ((((((12/4)+9)/6)+4)/8)/R)+2$$

$$R_{AB} = (((((3+9)/6)+4)/8)/R)+2 = (((((12/6)+4)/8)/R)+2 = (((4+4)/8)/R)+2 = (4R/(4+R))+2$$

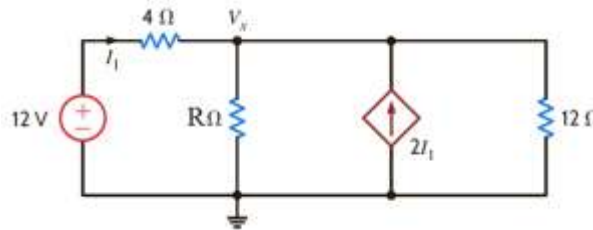
Version A; $R=8\text{k}\Omega$, then $R_{AB}= 4.7 \text{ k}\Omega$

Version B; $R=12 \text{ k}\Omega$, then $R_{AB}= 5 \text{ k}\Omega$

Version C; $R=16 \text{ k}\Omega$, then $R_{AB}= 5.2 \text{ k}\Omega$

Problem 2 (4 pts)

Determine the power dissipated in the $R \Omega$ resistor in the network shown below.



Node equation for V_x

$$\frac{V_x - 12}{4} + \frac{V_x}{R} + \frac{V_x}{12} - 2 \left(\frac{12 - V_x}{4} \right) = 0$$

Solving for V_x , we obtain

$$V_x = 108 * \left(\frac{R}{10R+12} \right) \text{ and } Pr = \frac{(V_x)^2}{R}$$

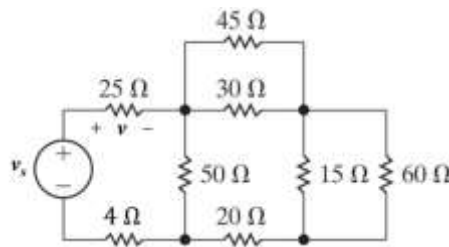
Version A: $R=6 \Omega$, $V_x=9 \text{ Volts}$, and $P = \frac{V_x^2}{R}=13.5 \text{ W}$

Version B: $R=9 \Omega$, $V_x=9.53 \text{ Volts}$, and $P = \frac{V_x^2}{R}=10.1 \text{ W}$

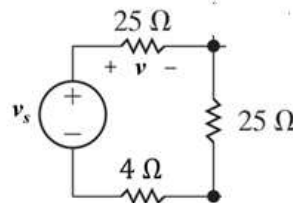
Version C: $R=12 \Omega$, $V_x=9.82 \text{ Volts}$, and $P = \frac{V_x^2}{R}=8.04 \text{ W}$

Problem 3 (4 pts)

Find v (voltage drop across the $25\ \Omega$ resistor), when $v_s = 15\ \text{V}$.



Simplifying the above circuit, $(15 \parallel 60 + 45 \parallel 30 + 20) \parallel 50 = (12 + 18 + 20) \parallel 50$ we obtain



Using Voltage divider rule, we obtain: $v = v_s \frac{25}{54}$

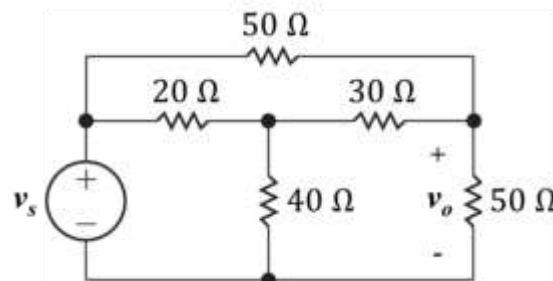
Version A: For $v_s = 15\ \text{V}$, then $v = 6.94\ \text{V}$

Version B: For $v_s = 25\ \text{V}$, then $v = 11.57\ \text{V}$

Version C: For $v_s = 15\ \text{V}$, then $v = 6.94\ \text{V}$

Problem 4 (4 pts)

Solve the circuit below, find v_o . Take $v_s = 21\ \text{V}$.



Grounding the negative terminal of the voltage source, the two nodal equations read:

$$\frac{V_A - v_s}{20} + \frac{V_A}{40} + \frac{V_A - v_o}{30} = 0$$

$$\frac{v_o - V_A}{30} + \frac{v_o}{50} + \frac{v_o - v_s}{50} = 0$$

Solving, we obtain

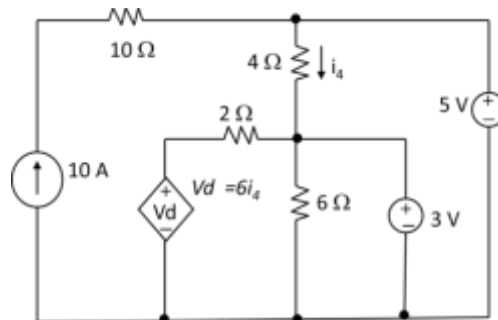
Version A: For $v_s = 21$, $v_o = 11.78\ \text{V}$

Version B: For $v_s = 24$, $v_o = 13.46\ \text{V}$

Version C: For $v_s = 35$, $v_o = 19.6\ \text{V}$

Problem 5 (4 pts)

Find the power supplied/absorbed by the 3V source



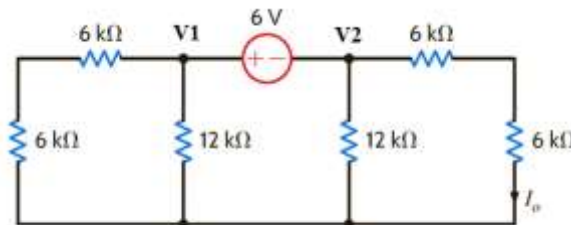
The current $i_d = (5-3)/4 = 0.5$ A. The Voltage $V_d = 3$ volts. The current in the 2Ω resistor is 0A. The current in the 6Ω resistor is 0.5 A.

Using KCL, the current leaving the 3V source is 0 A. Therefore, the power associated with this source is 0Watts.

The answer is: None of the above for all versions (0)

Problem 6 (7 pts)

We want to determine the value of I_0 in the circuit shown below:



- a. Write nodal equations for the node voltages V_1 and V_2 . (2 pts)

$$\frac{V_1}{12} + \frac{V_1}{12} + \frac{V_2}{12} + \frac{V_2}{12} = 0 \xrightarrow{\text{yields}} 2V_1 + 2V_2 = 0 \quad (1)$$

$$V_1 - V_2 = 6 \quad (2)$$

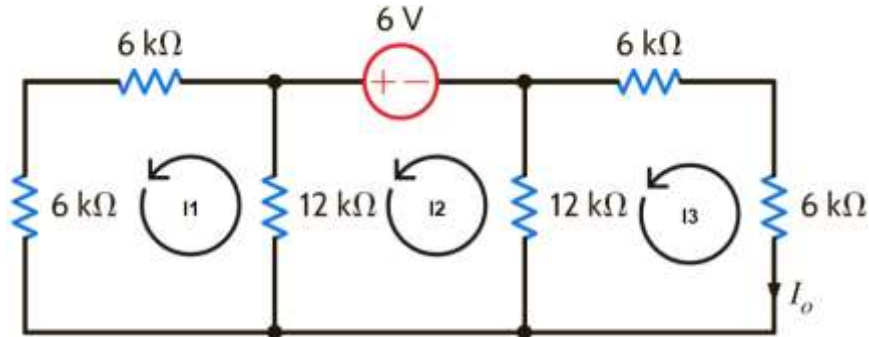
- b. Solve for the node voltage V_1 and V_2 . (1 pt)

$$V_1 = 3 \text{ V} \quad V_2 = -3 \text{ V}$$

- c. Deduce the current I_0 (1 pt)

$$I_0 = \frac{V_2}{12 * 1000} = -0.25 \text{ mA}$$

- d. Resolve the circuit using mesh analysis and write the three mesh equations.(3 pt)



$$\text{Mesh 1: } 24I_1 - 12I_2 + 0I_3 = 0$$

$$\text{Mesh 2: } -12I_1 + 24I_2 - 12I_3 = 6$$

$$\text{Mesh 3: } 0I_1 - 12I_2 + 24I_3 = 0$$

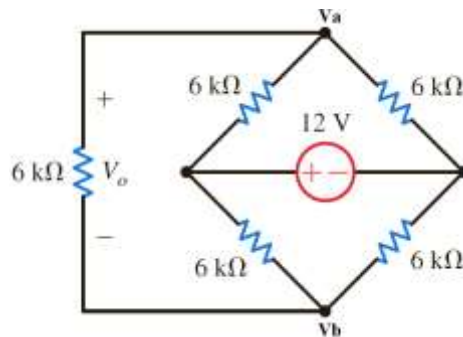
Solving 1, 2, and 3 yields: $I_1 = 0.25 \text{ mA}$, $I_2 = 0.5 \text{ mA}$, $I_3 = 0.25 \text{ mA}$.

- e. Verify the value of I_0 obtained in (c). (1 pt)

$$\text{Therefore } I_0 = -I_3 = -0.25 \text{ mA}$$

Problem 7 (6 pts)

We would like to find the value of V_0 in the circuit below,



- a. Write the node voltage equation. (3 pts)

$$\frac{V_a}{6} + \frac{V_a - 12}{6} + \frac{V_a - V_b}{6} = 0$$

$$\frac{V_b - V_a}{6} + \frac{V_b}{6} + \frac{V_b - 12}{6} = 0$$

- b. Solve for voltages V_a and V_b . (2 pts)

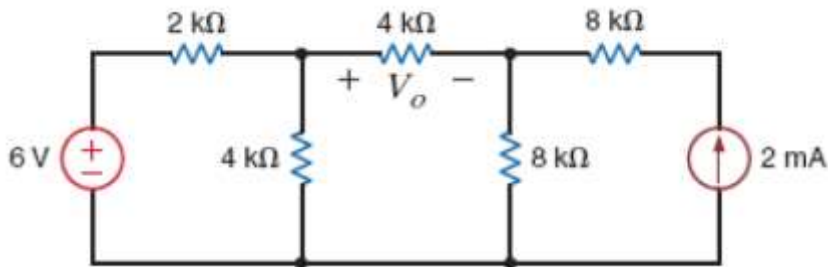
$$V_a = V_b = 6 \text{ Volts}$$

- c. Deduce the value of V_0 (1 pt)

$$V_0 = V_a - V_b = 0 \text{ Volts}$$

Problem 8 (5 pts)

We would like to find the value of V_0 in the circuit below:



- a. Would you use mesh or nodal analysis? Why? (1 pt)

Two nodes vs 3 branches. Nodal analysis.

- b. Solve for V_0 using the method you specified in a. (4 pts)

$$\frac{V_1 - 6}{2} + \frac{V_1}{4} + \frac{V_1 - V_2}{4} = 0$$

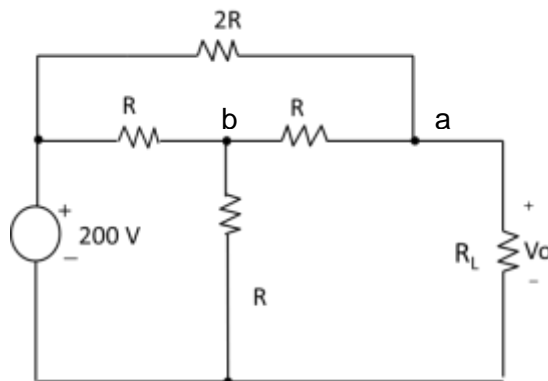
$$\frac{V_2 - V_1}{4} + \frac{V_2}{8} - 2 = 0$$

Solving, we obtain $V_1=5.2$ Volts and $V_2=8.8$ Volts .

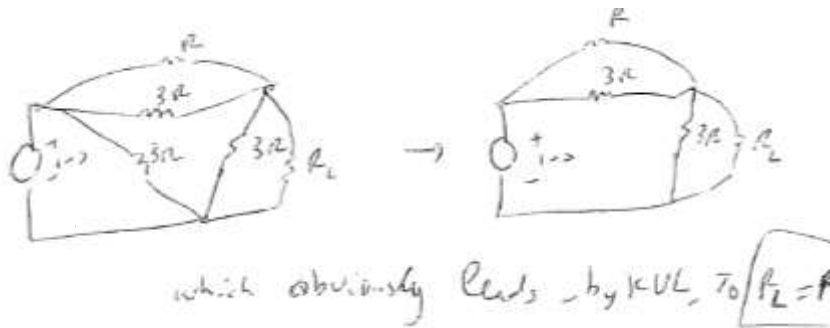
Therefore, $V_0=5.2 - 8.8 = - 3.6$ Volts

Problem 9 (6 pts)

Find R_L such that the voltage $V_0=100$ Volts



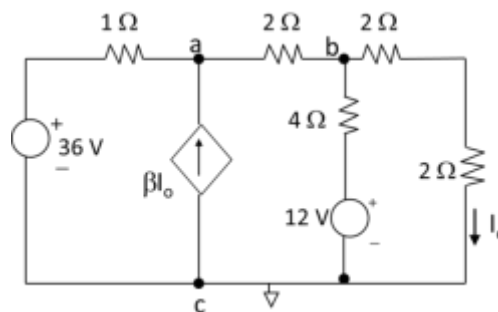
Transform the Y in the middle to a Delta:



$$\rightarrow R_L = 2R$$

Problem 10 (6 pts)

If you are told that node c is a reference ($V_c = 0$ Volts).



- a. Write nodal equations at nodes a and b. (3 pts)

$$\frac{V_a - 36}{1} + \frac{(V_a - V_b)}{2} - \beta I_o = 0$$

$$\frac{(V_b - V_a)}{2} + \frac{(V_b - 12)}{4} + \frac{(V_b)}{4} = 0$$

- b. Find β such that $V_b = 12$ Volts. (3 pts)

$$I_o = \frac{(V_b)}{4} = 3 \text{ A. Solving for 1 and 2, we obtain: } \beta = -5$$

OR from first principles:

$V_b = 12 \text{ V}$, then $I_{4\Omega} = 0$, so $I_{a \rightarrow b} = I_o$; Now KCL at node a: $I_{a \rightarrow b} = \beta I_o + I_{36V}$, then

$$I_{36V} = \frac{36 - 6I_o}{1} = 18A$$

$$\text{So } \beta = (-18/I_o) + 1 = -5$$